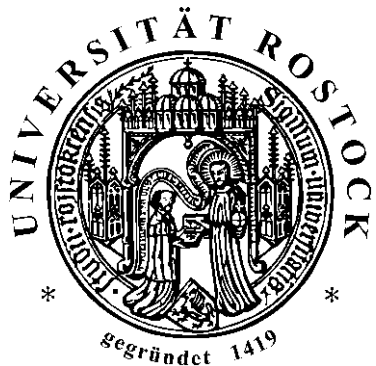
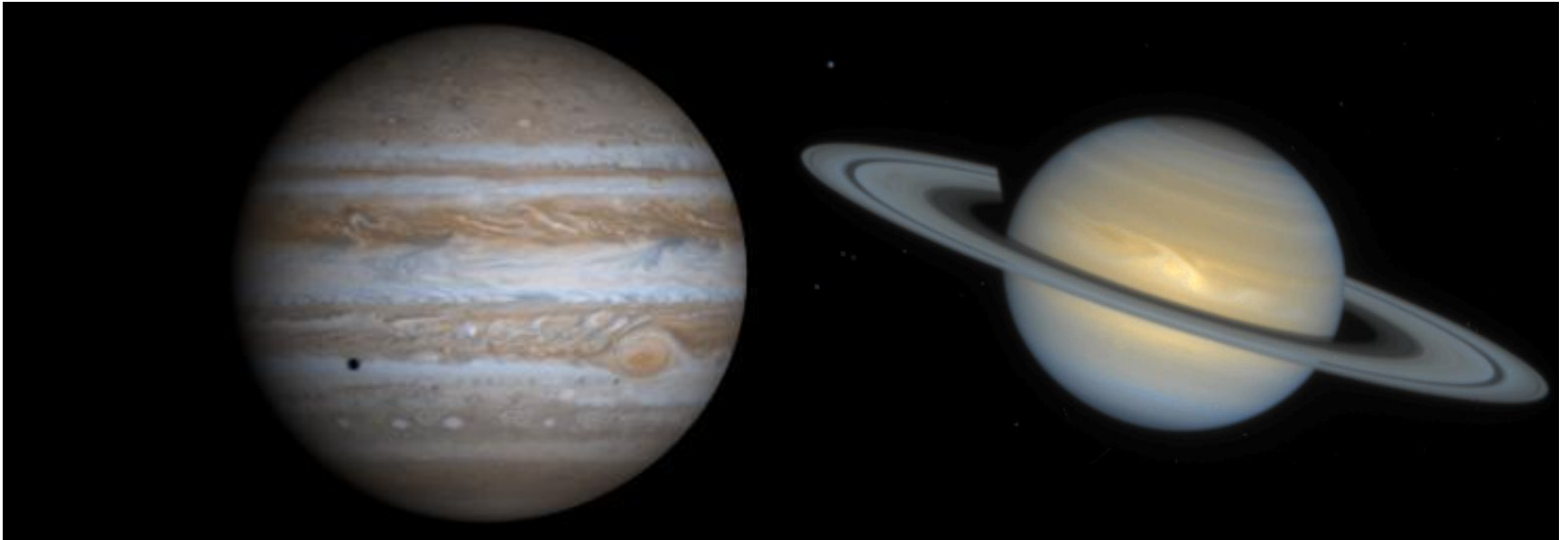


YETI Workshop in Jena, 15-17 November 2010

# The Interior of Giant Planets



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# CO-WORKERS

## **AIMD simulations:**

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*M.P. Desjarlais, T.R. Mattsson (Sandia Natl. Lab.)*

## **Giant planets:**

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*R. Neuhäuser (U Jena)*

*J.J. Fortney (Santa Cruz)*

*D.J. Stevenson (Pasadena)*

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Computing Center of the University of Rostock

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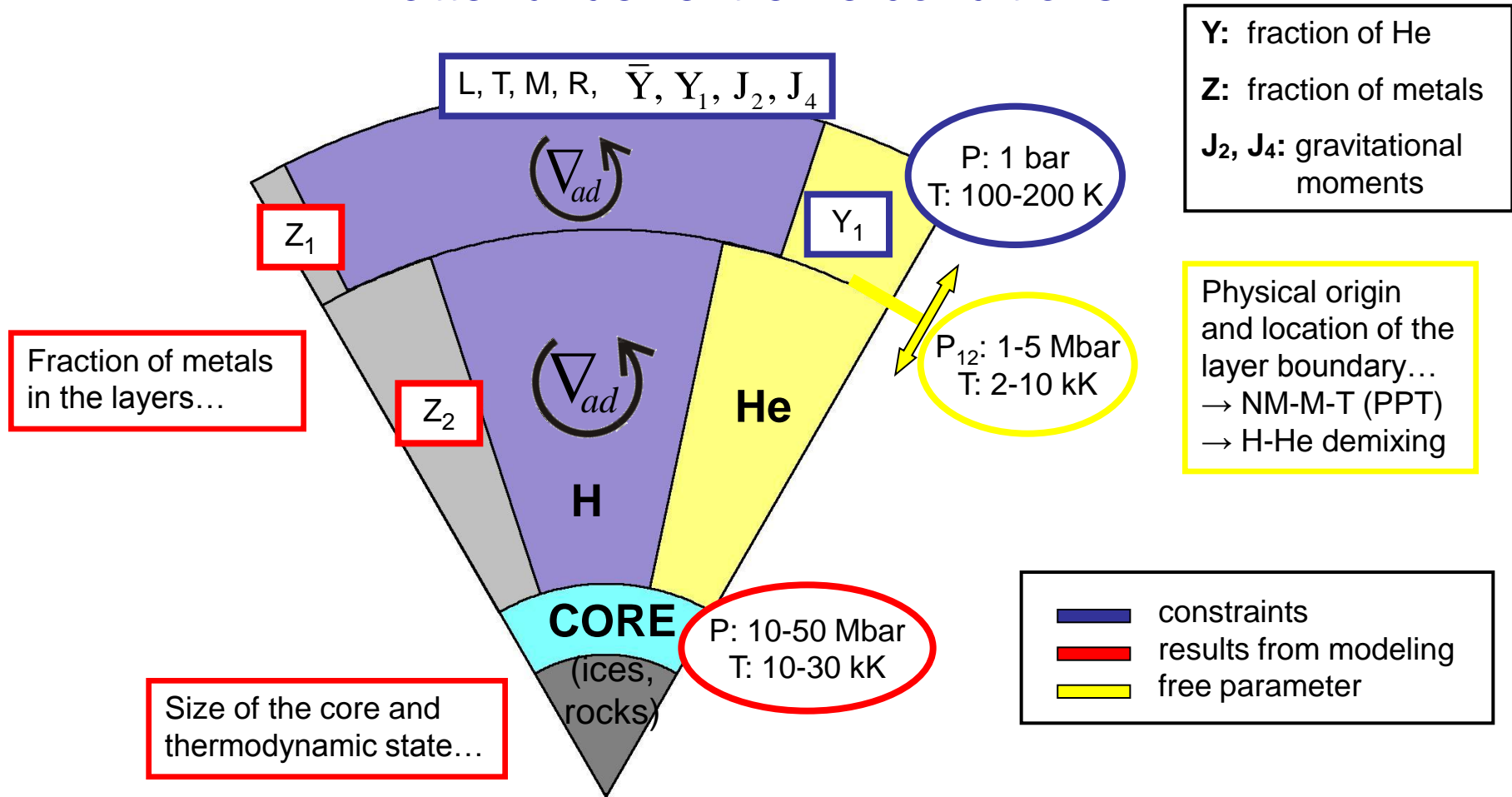
## **4. Interior of solar and extrasolar GPs**

*Results*

## **5. Summary**

# Interior of solar giant planets:

Matter under extreme conditions!



- Three-layer interior models are uniquely defined by the observables, except  $P_{12}$
- Input: EOS data for warm dense H and He, metals (C-N-O), and the isothermal rocky core
- Predictions of chemical models and new ab initio simulation data

# Basic equations for planetary modeling

mass conservation:

$$dm = 4\pi r^2 \rho(r) dr$$

hydrostatic equation of motion:

$$\frac{1}{\rho} \frac{dP}{dr} = \frac{dU}{dr}, \quad U = V + Q$$

gravitational potential:

$$V(\vec{r}) = -G \int_{V_0} d^3 r' \frac{\rho(r')}{|\vec{r} - \vec{r}'|}$$

expansion into Legendre polynomials:

$$V(r, \theta) = -\frac{GM}{r(\theta)} \left( 1 - \sum_{i=1}^{\infty} \left( \frac{R_{eq}}{r(\theta)} \right)^{2i} J_{2i} P_{2i}(\cos \theta) \right)$$

gravitational moments:

$$J_{2i} = -\frac{1}{MR_{eq}^{2i}} \int d^3 r' \rho(r'(\theta')) r'^{2i} P_{2i}(\cos \theta')$$

Calculations via theory of figures (Zharkov & Trubitsyn).

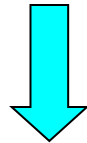
Planetary interior program: N. Nettelmann (2009).

**Mass distribution along isentropes according to the EOS data used for the relevant materials (H, He, C-N-O, rocks).**

# EOS and phase diagram of light elements at high pressures ?

Poorly known above 1 Mbar but important for interior models: EOS data, isentropes, origin and location of layer boundaries, conductivity and magnetic field structure, opacity etc

Apply ab initio methods and novel high-pressure experiments e.g. at NIF, Z for conditions deep in planetary interiors, i.e. for  
→ 1-100 Mbar and  $10^3$ - $10^5$  K  
→ light elements, their hydrides and mixtures (H, He, H-He, H<sub>2</sub>O, CH<sub>4</sub>, NH<sub>3</sub> ...)



- 1. Metallization in H: 1st-order phase transition (PPT)?**
- 2. Is there a H-He demixing region as proposed earlier?**
- 3. Superionic phases at high pressures (H<sub>2</sub>O)?**

# Ab initio MD (AIMD) simulations for WDM

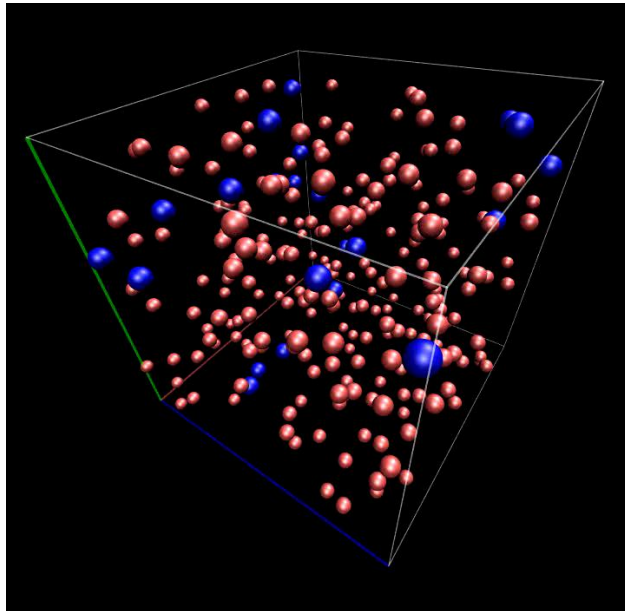
Born-Oppenheimer approximation: combination of (quantum) DFT and (classical) MD  
WDM: finite-temperature DFT-MD simulations based on

N.D. Mermin, *Phys. Rev.* **137**, A1441 (1965)

Implemented e.g. in the Vienna Ab-initio Simulation Package (VASP)

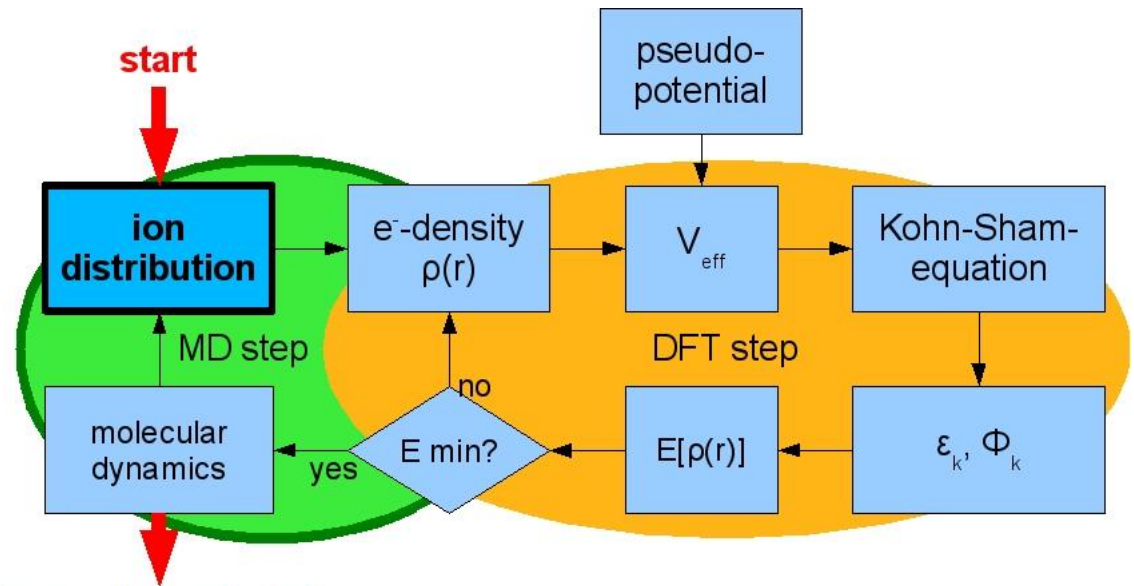
G. Kresse and J. Hafner, *PRB* **47**, 558 (1993), *ibid.* **49**, 14251 (1994)

G. Kresse and J. Furthmüller, *Comput. Mat. Sci.* **6**, 15 (1996), *PRB* **54**, 11169 (1996)



H-He (8.6%) @ 1 Mbar, 4000 K

box length  $\sim 10^{-9}$  m



thermodynamic data  
pair correlation functions  
electrical conductivity  
diffusion coefficients  
high-pressure phase diagram



GP size  $\sim 10^8$  m

# Some details of the AIMD simulations

VASP: G. Kresse et al., Phys. Rev. B **47**, 558 (1993)

- Plane wave basis set: energy cut-off at about 1 keV
- **Exchange-correlation functional: GGA [1]**
- **PAW pseudopotentials [2]: 1 e/H, 2 e/He, 6(8) e/O**
- Ion temperature control by Nosé thermostat [3]
- Evaluation of electronic states in BZ at (few) special points (EOS)
- Higher k-point sets are needed for  $\sigma$
- **$N \leq 1024$  electrons in a box of volume  $V$  at temperature  $T$**
- **Simulation time: up to 20 ps with several 1000 time steps**
- **Check convergence with respect to  $E_{\text{cut}}$ , k-points,  $N$ ,  $\Delta t$  ...**
- Parallel code runs on “Mercury” at Computing Center U Rostock
- CPU time at High Performance Computing Center North (HLRN)

[1] J.P. Perdew, K. Burke, M. Ernzerhof, PRL **77**, 3865 (1996)

[2] P.E. Blöchl, PRB **50**, 17953 (1994), G. Kresse, J. Joubert, PRB **59**, 1758 (1999)

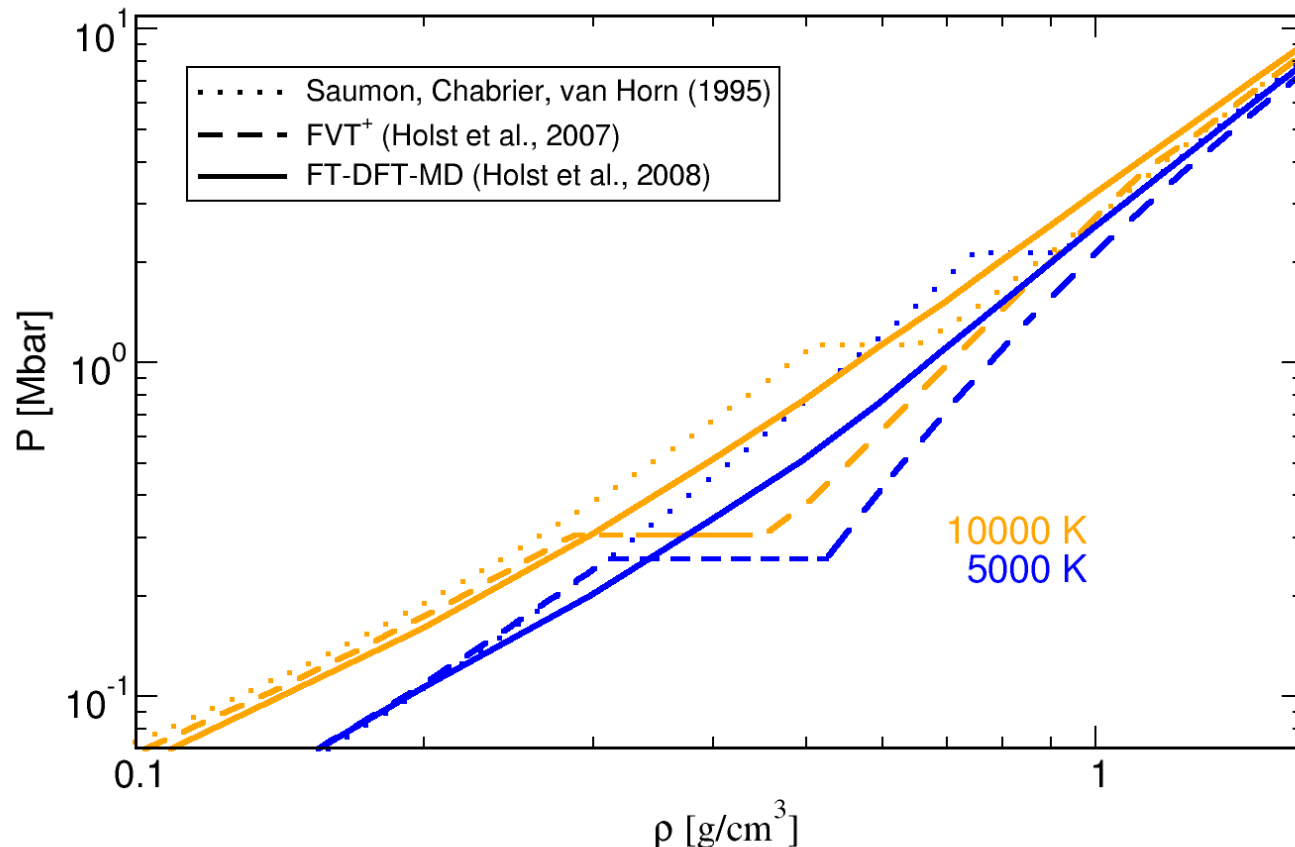
[3] S. Nosé, J. Chem. Phys. **81**, 511 (1984)



# Example: EOS of warm dense H2

AIMD compared with chemical models – no PPT above 5000 K

B. Holst, R. Redmer, M.P. Desjarlais, PRB **77**, 184201 (2008)

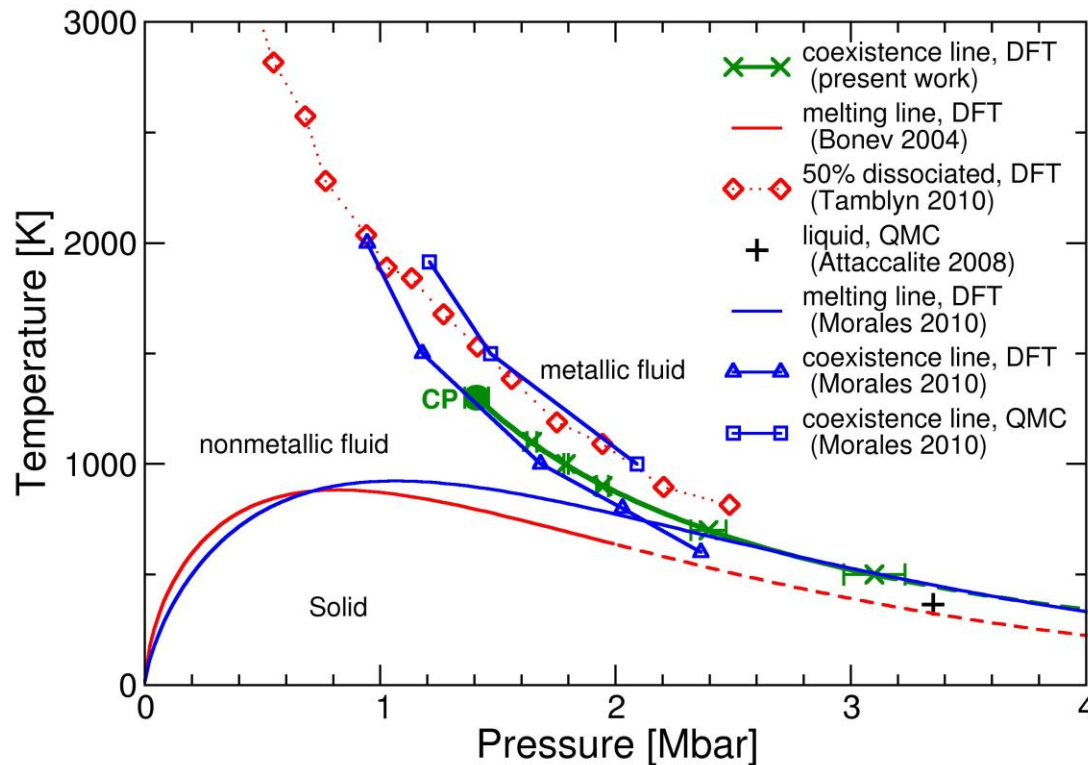


First exp. signature of a PPT ? See V.E. Fortov et al., PRL **99**, 185001 (2007)

AIMD EOS data on H2/D2: see also e.g. L. Collins et al., PRE **52**, 6202 (1995), S.A. Bonev et al., PRB **69**, 014101 (2004), F. Gygi and G. Galli, PRB **65**, 220102(R) (2002). QMC method: K.T. Delaney et al., PRL **97**, 235702 (2006).

# New hydrogen phase diagram at high pressure:

## 1st-order liquid-liquid phase transition (PPT)



**1st-order liquid-liquid phase transition has been predicted below 2000 K:**

M.A. Morales et al., PNAS **107**, 12799 (2010): AIMD and QMC;  
see also I. Tamblyn, S.A. Bonev, PRL **104**, 065702 (2010)

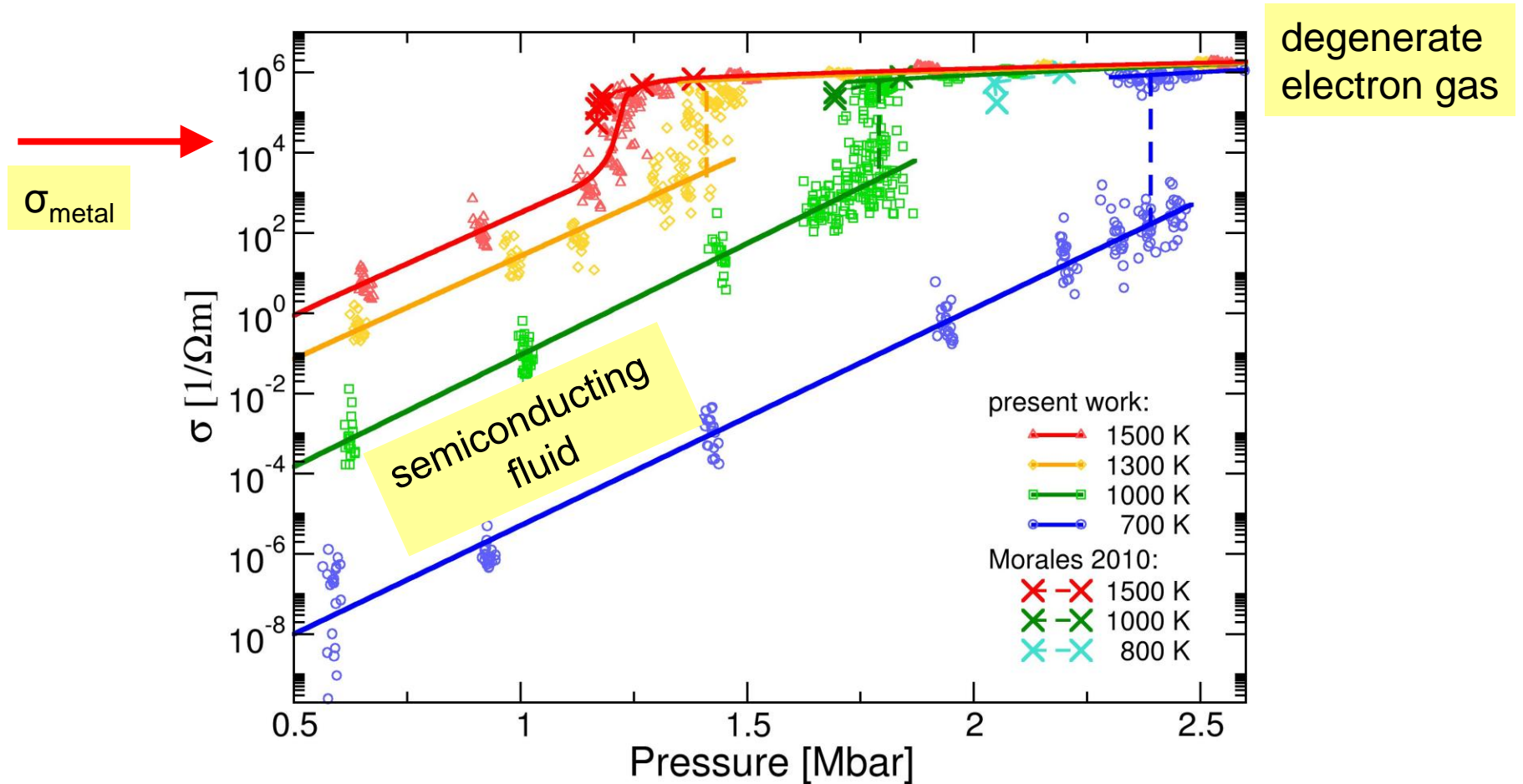
**We confirm these results with special emphasis to the NM-M-T:**

critical point located below 1500 K at 0.82 g/ccm, 1.4 Mbar  
W. Lorenzen, B. Holst, R. Redmer PRB **82**, 195107 (2010)

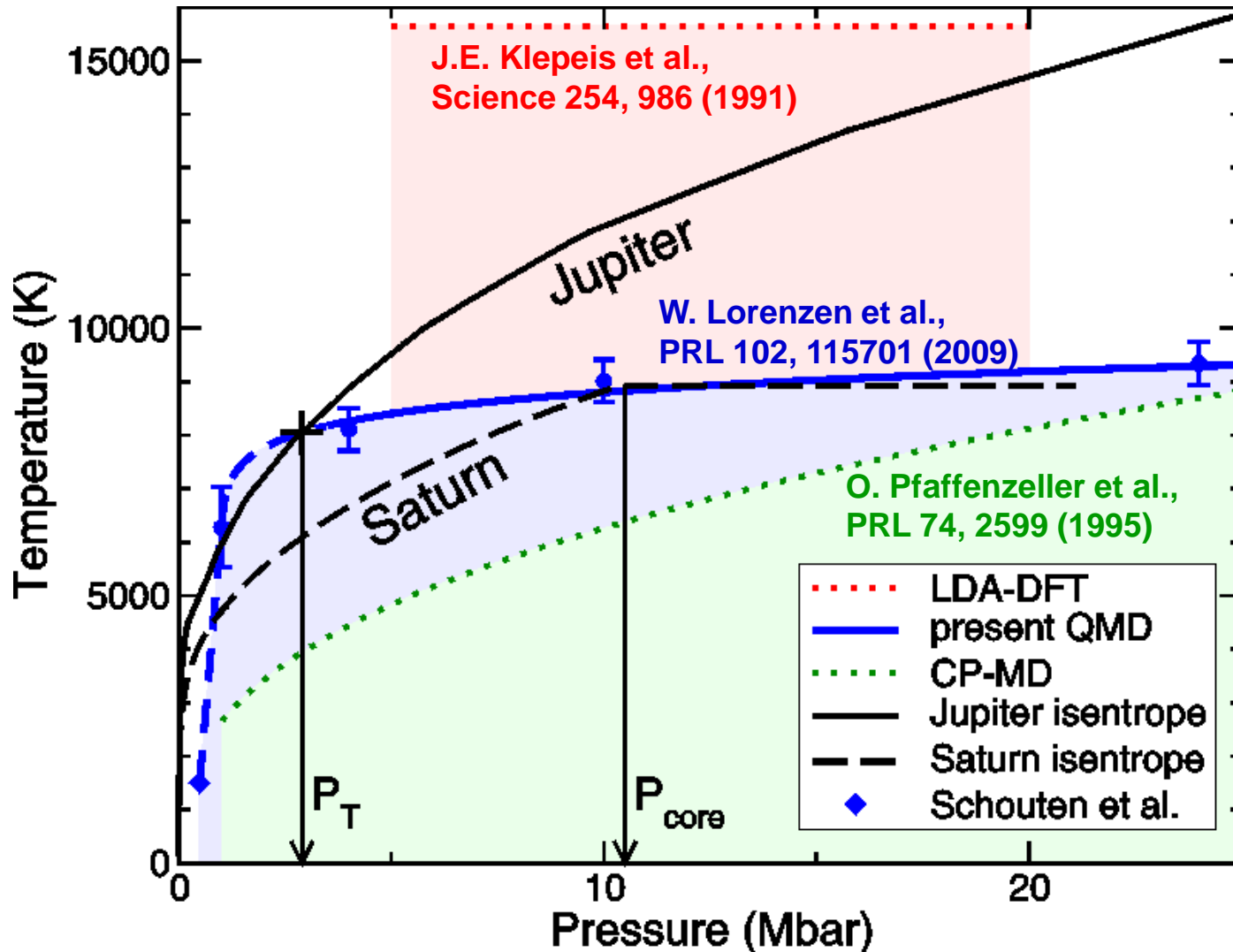
# Electrical conductivity in liquid hydrogen

NM-M-T drives the 1st-order phase transition

Continuous above critical point - along the Jupiter isentrope

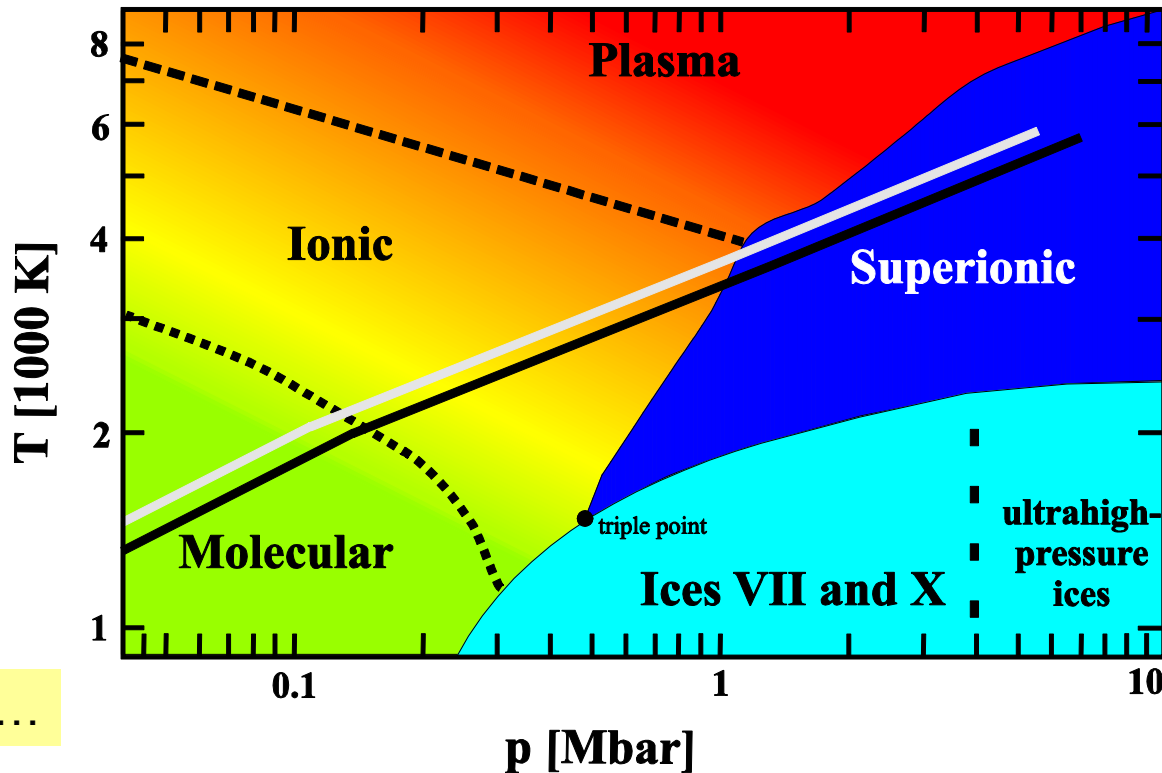


# Consequences of the NM-M-T for GPs: Demixing of H-He - relevant for Jupiter (?) and Saturn (!)



Similar results by M.A. Morales et al., PNAS 106, 1324 (2009) based on DFT-MD.

# Water phase diagram at ultra-high pressures



Relevant for the interiors of Neptune (black) and Uranus (white)

Representative of metals in J & S (Z)

Core material?

... and superionic water at 7 g/cm<sup>3</sup> and 6000 K

Normal ice...

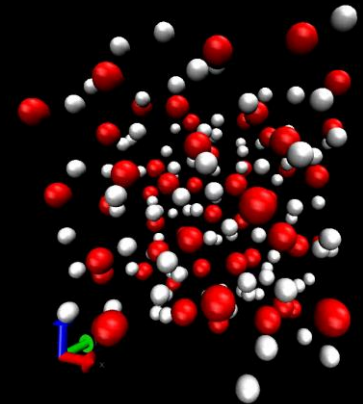
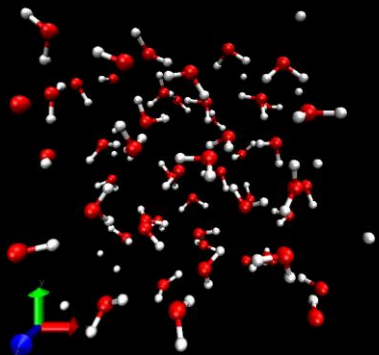
EOS and phase diagram:

M. French et al., PRB **79**, 054107 (2009)

Transport properties (diffusion, conductivity):

M. French et al., PRB **82**, 174108 (2010)

see also C. Cavazzoni et al., Science **283**, 44 (1999),  
T.R. Mattsson, M.P. Desjarlais, PRL **97**, 017801 (2006),  
E. Schwegler et al., PNAS **105**, 14779 (2008)



# Interior of Jupiter with LM-REOS

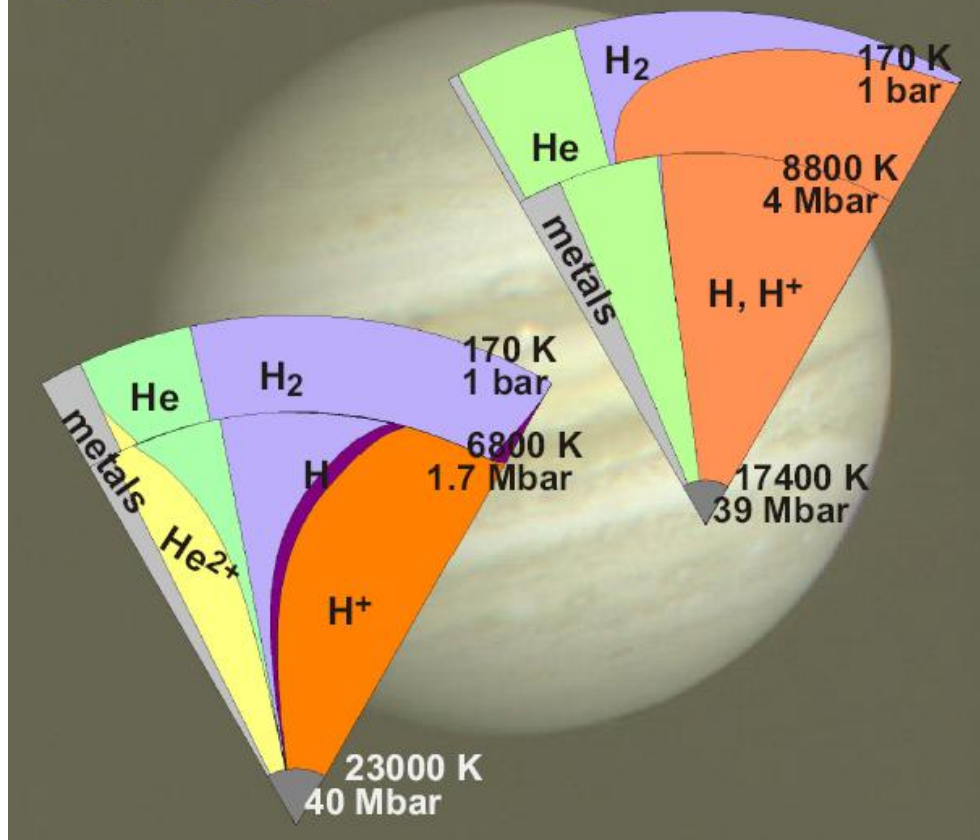
N. Nettelmann et al., ApJ **683**, 1217 (2008)

Alternative two-layer Jupiter model by B. Militzer et al., ApJ 688, L45 (2008)

## Abundances of chemical species for 2 models using different EOS

H, He : SCvH-ppt  
Core : rocks

H, He : QMD



Ab initio LM-REOS based on a strict physical picture covers 97% of Jupiter mass:

- strong discontinuity in metals
- earlier onset of 'ionization'
- also small core with  $M_c = (1-6) M_E$
- $P_{12}$  around 4 Mbar
- reason for the layer boundary:

**H-He phase separation?**

**as proposed earlier by Stevenson, Salpeter, Fortney, Hubbard ...**

Standard SCvH-EOS within an advanced chemical model:

- well separated 'molecular' and 'metallic' layer
- $P_{12}$  around 1.7 Mbar
- metals almost uniformly distributed
- reason for the layer boundary:

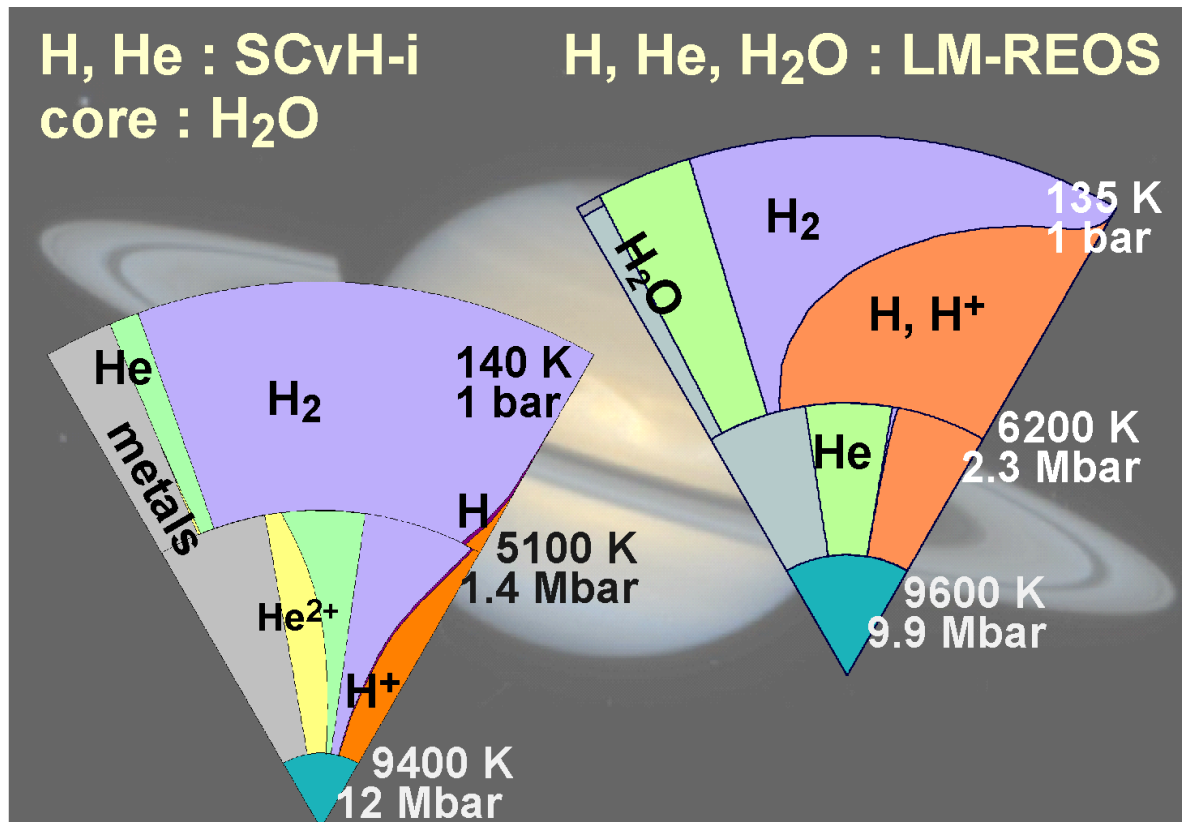
**plasma phase transition in H?**

H-He EOS of D. Saumon, G. Chabrier, H.M. Van Horn, ApJS **99**, 713 (1995)

H<sub>2</sub>O EOS from Sesame tables (1972)

# Interior of Saturn with LM-REOS

J.J. Fortney, N. Nettelmann, Space Sci. Rev. **152**, 423 (2009)



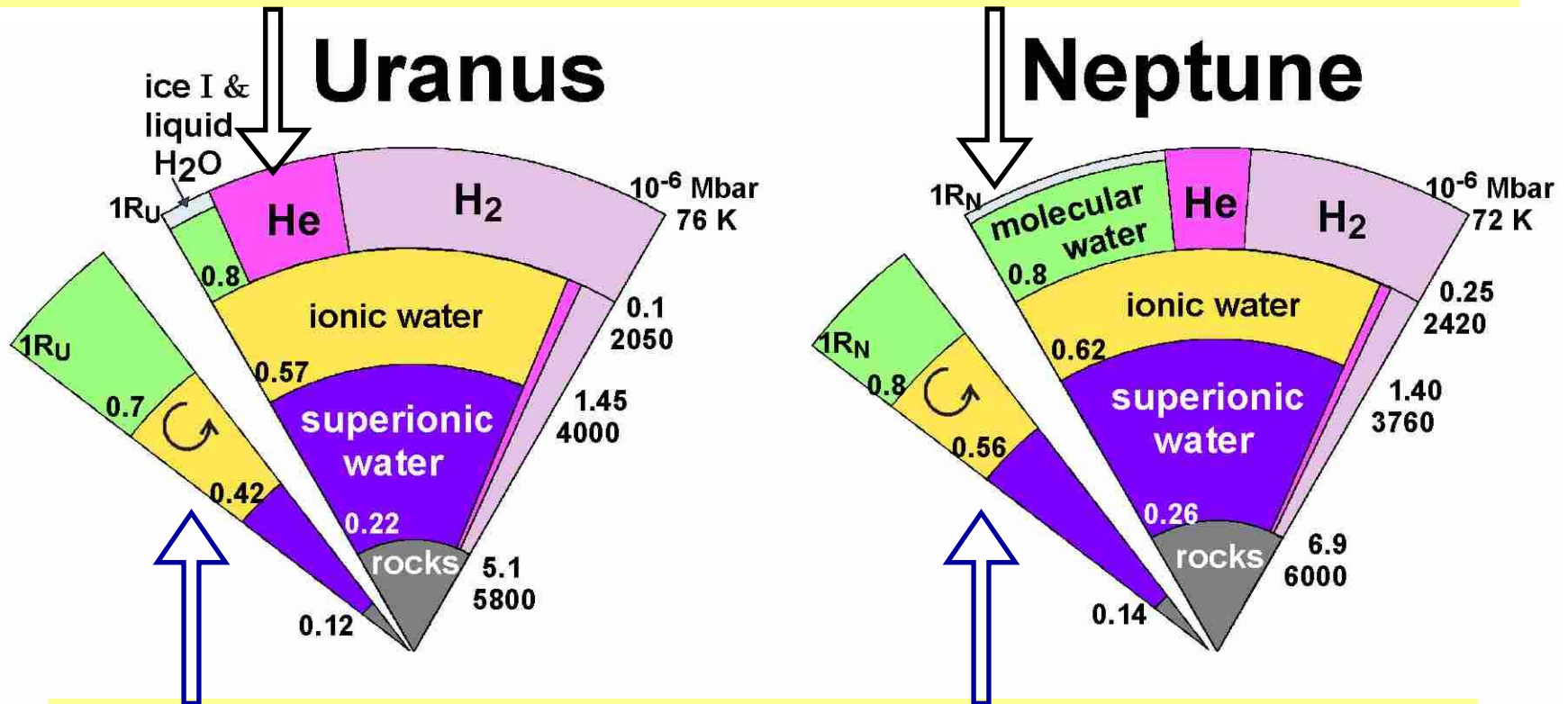
## Saturn's interior in comparison with that of Jupiter:

- lower temperatures → larger molecular outer envelope
- strong candidate for H-He demixing → higher luminosity and age?
- higher fraction of metals (up to 40%)
- greater core → superionic water in the core?

# Interior of Neptune and Uranus

Our **interior models** reproduce the gravity data based on the EOS and the phase diagram of H<sub>2</sub>O and H, He (LM-REOS):

J.J. Fortney, N. Nettelmann, *Space Sci. Rev.* **152**, 423 (2009),  
R. Redmer et al., *Icarus* (in print)



Independent **dynamo models** reproduce the non-dipolar and non-axisymmetric magnetic fields of N and U by assuming a rather thin conducting shell (yellow) and a central region (magenta) that is stable against convection but of similar conductivity (here: superionic!):

S. Stanley and J. Bloxham, *Nature* **428**, 151 (2004).



# Hot Neptune GJ 436b

Mass-radius relation for transiting planets known (plus radial velocity method)

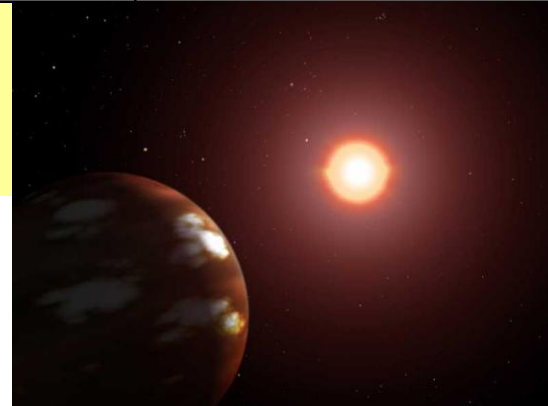
	Neptune	GJ 436b
mass [ $M_{\oplus}$ ]	17.13	$22.6 \pm 9\%$
radius [ $R_{\oplus}$ ]	3.86	$3.95 \pm 9\%$
surface temperatur [K]	70 (at 1 bar)	$520 (T_e) - 720 (8 \text{ } \odot m)$
semi major axis [AU]	30	0.03
period	165 years	2.64 days

Host star is M Dwarf with  $T_{\text{eff}}=3350$  K and  $M=0.44 M_{\text{Sun}}$ , 33 Ly away (Leo)  
H.L. Maness et al., PASP **119**, 90 (2007)

Observational parameters:

M. Gillon et al., A&A **471**, L51 (2007),

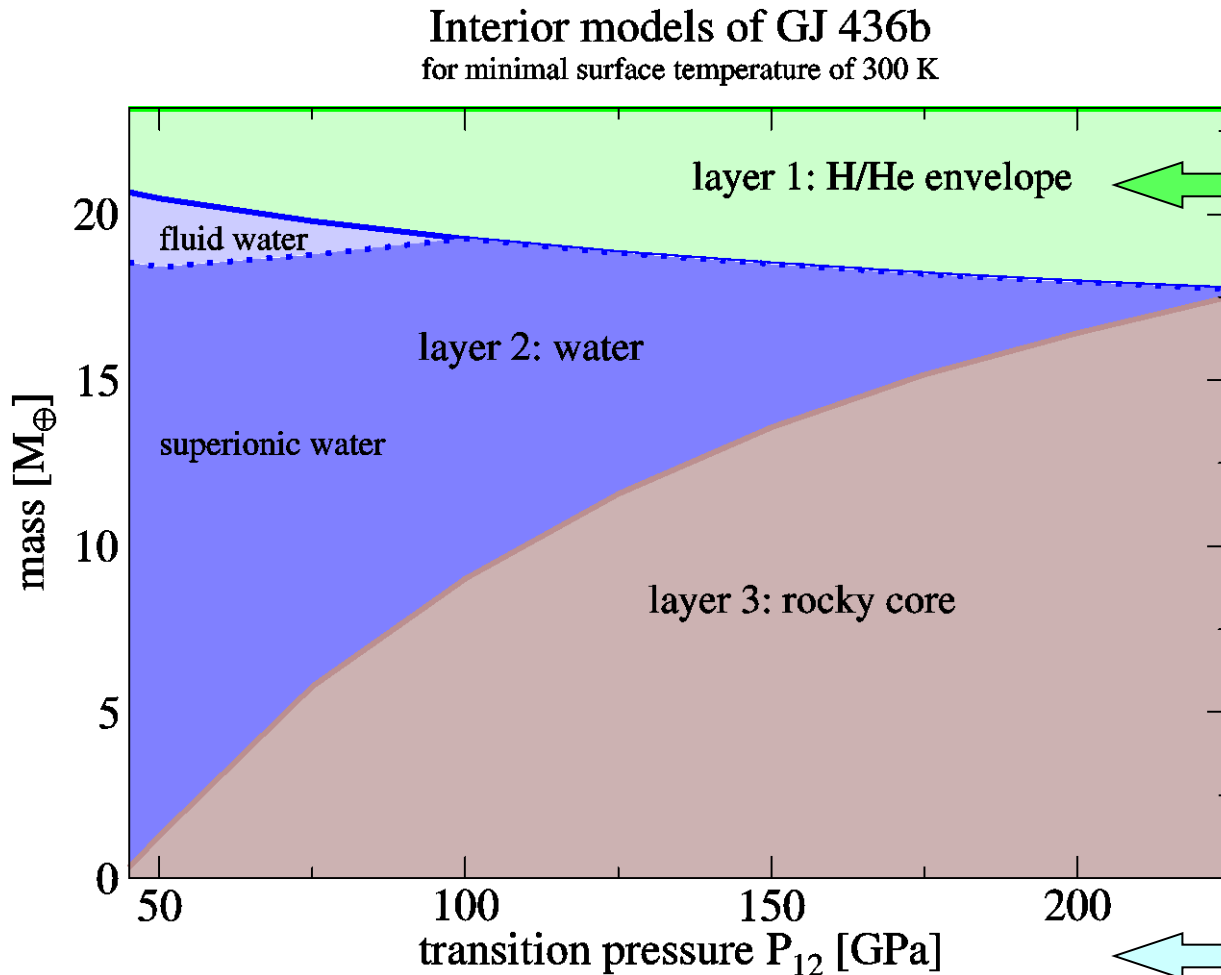
B.-O. Demory et al., A&A **475**, 1125 (2007)



# GJ 436b: Water or rocky planet?

What information can we derive from a known  $M(R)$  relation within a three-layer model?

N. Nettelmann et al.,  
A&A **523**, A26 (2010)



Isothermal  $H_2$ -He  
mixture (27.5%):  
 $T(1 \text{ bar})=300 \text{ K}$   
 $Z_1=2\%$   
high metallicity

Results of modelling  
**strongly** depend on  
surface temperature!  
Coupling of planetary  
atmosphere to stellar  
radiation important!

Limiting cases by  
varying  $P_{12}$  yield  
**water or rocky  
planet**. Is the water  
superionic ?

# Summary

- Paramount importance for modeling GPs:
  - accurate high-pressure EOS data: LM-REOS
  - identify the phase diagram and coexistence lines
  - compare with shock compression experiments
- Develop and evaluate interior models:
  - solar GPs
  - determine material data ( $\sigma$ ,  $\eta$ ,  $c_s$  ...) along the isentropes
  - additional constraint: *U. Kramm, Love number  $k_2$*
  - extrasolar GPs: *N. Nettelmann, GJ 1214b*
- Young transiting planets: *R. Neuhäuser et al., YETI*
- Planetary atmospheres: *P. Hauschildt et al., J.J. Fortney*
- Planetary magnetism: *DFG-SPP 1488*