

## Perturbation equations in Hamiltonian form

$$\begin{aligned}\frac{dL_k}{dt} &= \frac{\partial \mathcal{H}}{\partial l_k}, \\ \frac{dl_k}{dt} &= -\frac{\partial \mathcal{H}}{\partial L_k},\end{aligned}\quad (k = 1,2,3)$$

with the Hamiltonian

$$\mathcal{H} = \frac{\mathfrak{a}^4}{2L_1^2} + R$$

and the *Delaunay variables*

$$\begin{aligned}L_1 &= \mathfrak{a}\sqrt{a}, & l_1 &= M, \\ L_2 &= \mathfrak{a}\sqrt{a(1-e^2)}, & l_2 &= \omega, \\ L_3 &= \mathfrak{a}\sqrt{a(1-e^2)} \cos I, & l_3 &= \Omega\end{aligned}$$